

## **Workshop 20200201 – Information for Ian.**

**Material covered in my presentation: Please post that students and parents can review (I did not use math symbols in this presentation).**

### **Parts of the whole:**

**How much time does it take to fill up a pool with 3 taps (A, B, and C) if each takes 4, 5, and 7 hours respectively? Do the same if you have 2 taps (A and B) and one draining pipe in 3 hours. Express the answer as a fraction in lowest terms.**

### **Method**

**Let X be the number of hours. Then,**

$$1 = \frac{X}{4} + \frac{X}{5} + \frac{X}{7}$$

$$140 = (35 + 28 + 20) * X = 83X$$

$$X = 140/83$$

**For the second case: Let X be the number of hours. Then,**

$$1 = \frac{X}{4} + \frac{X}{5} - \frac{X}{3}$$

$$60 = (15 + 12 - 20) * X = 7X$$

$$X = 60/7$$

### **Mixtures**

**Bag A has 20 kg of which 45% is sand (by weight) and the rest is pebbles. You combine it with another bag B and that also has mixture of sand and pebbles. The weight of the combined mixture is 50 kg with 50% sand (by weight). What percentage of pebbles were in bag B? Round the answer to the nearest whole number.**

### **Method**

**Total weight of sand in bag A: 9 kg.**

**Total weight of sand in combined mixture: 25 kg.**

**Weight of Bag B: 50-20=30 kg.**

**Weight of sand in bag B: 25-9=16 kg.**

**Weight of pebbles in bag B: 30-16=14 kg.**

**Percentage of pebbles in bag B:  $(14/30)*100=140/3$ , or 46.666...  
Round to whole number: 47**

**Polygons, angles and their sum.**

**Acute angle: less than 90 deg**

**Right angle: 90 deg**

**Obtuse angle: more than 90 deg and less than 180 deg**

**Convex polygon: all angles are less than 180 deg**

**Sums of all angles of a polygon with N sides.**

**Polygon with N sides can be divided into N-2 triangles.**

**So total sum of angles is  $(N-2)*180$**

**Regular polygon: all angles and all sides are the same.**

**Examples are equilateral triangle and square.**

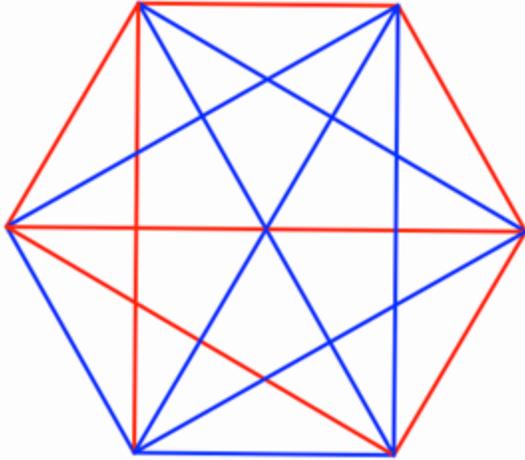
**What is the value of each angle for a regular polygon?**

**So, value of each angle is  $((N-2)*180)/N$**

**Congruent triangles: two triangles are congruent if all their sides have the same values.**

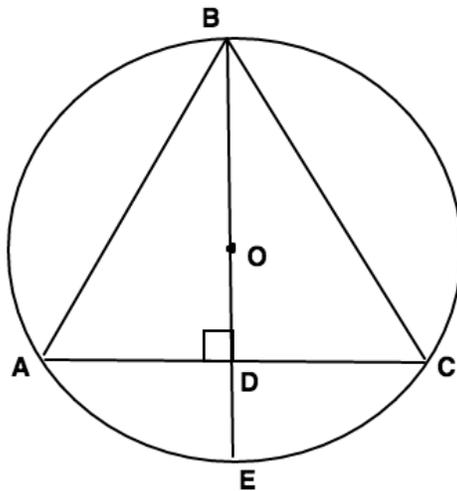
**Similar triangles: two triangles are similar if all their angles have the same values.**

**How many non congruent triangles can be formed using entire sides and/or entire lengths of diagonals of a regular hexagon?**



**3 Options:**

- a) Two sides and 1 diagonal: 1
- b) One side and 2 diagonals: 1
- c) Three diagonals: 1



**What is the area of equilateral triangle inscribed in a circle with area  $\pi$ ?**

**Area of circle is  $\pi = \pi * r * r$ . So,  $r = 1$**

**$OA = r = 1$ ,  $OD = 1/2$ ,  $h = 1/2 + 1 = 3/2$ ,  $AD = \sqrt{1 - 1/4} = \sqrt{3}/2$ , AC is side b of the triangle.  $b = AC = 2 * AD = \sqrt{3}$ ,**

**Area of triangle =  $(b * h) / 2 = (\sqrt{3} * (3/2)) / 2 = 3\sqrt{3} / 4$**

**My notes to the answers to 2020 Page 1 and Page 2 handouts:**

**Page 1:**

**#16.**

$$(X+15)/(X+25)=14/19$$

$$19*(X+15)=14*(X+25)$$

$$5X+5*15=14*10=140$$

$$5X=65$$

$$X/(X+10)=13/23$$

**#17.**

$$X/6+(7-X)/10=1$$

$$5X+21-3X=30$$

$$2X=9$$

$$X=9/2$$

**#18.**

$$(2^2-\pi^2/4)*4=(4-\pi)4$$

$$0.86*4 \text{ rounded to } 3.$$

**#19.**

$$0.95X-Y=5250, Y-0.75X=1750, 0.2X=7000, X=35000$$

$$0.75X+1750=26250+1750=28000$$

**#20.**

$$54.5+549.5=604$$

**Page 2:**

**#21.**

**Total is 16.**

**For 1-2 and 2-3 => 3-4, and 4-1. So 3 possibilities only for 1-2**

**Same for 1-3 and 1-4 so total is  $3*3=9$**

**#22.**

**Full pool has  $(2250*100)/75=3000$ . 80% pool has 2400.**

**Number of hours is  $2400/120=20$**

**#25.**

**$N=7*k^3$ ,  $2016=7*3^2*2^5$ , so  $7^2*k^3*3^2*2^5$  is a square, so  $k^3$  is square, so  $k=2$ , so  $N=7*8=56$**

**#26.**

**Sum of angles  $180*(5-2)=540$ .  $4N<180$ ,  $M=N*K/2<180$**

**$N*(1+2+3+4+K/2)=540=10N+NK/2=540$**

**If  $N=44 \Rightarrow NK/2=100$   $K/2=100/44$  NG (No Good).**

**If  $N=43 \Rightarrow NK/2=110$   $K/2=110/43$  NG.**

**If  $N=42 \Rightarrow NK/2=120$   $K/2=120/42$  NG.**

**If  $N=41 \Rightarrow NK/2=130$   $K/2=130/41$  NG.**

**If  $N=40 \Rightarrow NK/2=140$ ,  $K/2=3.5$ ,  $K=7$ .**

**If  $N=39 \Rightarrow NK/2=150$   $K/2=150/39$  NG.**

**If  $N=38 \Rightarrow NK/2=160$   $K/2=160/38$  NG.**

**If  $N=37 \Rightarrow NK/2=170$   $K/2=170/37$  NG.**

**$N=36$  is too small as  $10N=360$ .**

**So,  $M=40*7/2=140$**

**#4.**

**List of all subjects: 1,2,3,...,13.**

**1 and all primes are ok.**

**8,10,12 NG.**

**So, remaining are 4 (sum is  $1+2+4=7$ ), 6 (sum is  $1+2+3+6=12$ ),**

**9 (sum is  $1+3+9=13$ ).**

**So, from the number 1 and all primes we get**

**$1+3+4+6+8+12+14=48$**

**From the other three number we get  $7+12+13=32$**

**Total is  $48+32=80$**